





Visions of the Past, Present and Future of Statistical Graphics



Swiss Statistics Meeting, 2007 Michael Friendly York University, Toronto, CA



Slides: www.math.yorku.ca/SCS/Papers/swiss/

Outline

- Graphs as communication
- Success stories from the Golden Age
 - A.-M. Guerry & the invention of social science
 - The graphical vision of Ch. Jos. Minard
 - Galton's greatest graphical discovery
- Where are we today?
 - Graphs for data exploration & model fitting
 - Cognitive interfaces for models & graphics
- Where should we go in future?

Different graphs for different purposes



Exploration

Goal: the Wow! experience Single image for a large audience Goal: the Ah ha! Experience Many images, for a narrow audience (you!), linked to analysis 3

Different graphs for different purposes

- Graphs (& tables) as communication:
 - What is the audience?
 - What is the message?

• Analysis graphs: design to see patterns, trends, aid the process of data description, interpretation

• **Presentation graphs**: design to make a point, illustrate a conclusion



Presentation graph: Nightingale's coxcomb

Florence Nightingale: Deaths in the Crimean war from battle vs. other causes (disease, wounds)

She used this to argue for better field hospitals (MASH units)

The best presentation graphs pass the **Interocular Traumatic Test**: The message hits you between the eyes!



Rhetorical graph: Welfare income and Homeless deaths after the "Common Sense Revolution"



Analysis graph: Deaths vs. Income

Scatterplot of deaths vs. income

- Loess smooth + CI band
- · Labels: year
- Color: party in power

The message here is interesting, but it lacks the power and eloquence of the original graph



Context: Milestones Project

www.math.yorku.ca/SCS/Gallery/milestone



Project goals:

· Comprehensive catalog of developments in history of data visualization

· Tool to study themes, antecedents, influences, patterns, trends, etc.



1850-1900: Golden Age



Stories from the Golden Age (1850-1900)

Stories:

- Guerry & the invention of social science
- Graphic vision of C. J. Minard
- Galton's graphical discoveries
- Statistical albums

Themes:

- Statistics: numbers of the state
- Rise of visual thinking
- Visualization → Theory (graphic discovery)
- Theory \rightarrow Practice
- Graphical excellence

A.-M. Guerry and the invention of social science

André-Michel Guerry (1802-1866)

- *Essai* presented to Academie des Sciences Français: July 2, 1832
- First analysis of comprehensive data on crime, suicide, other 'moral' variables.

 Along with Quetelet, established the study of "moral statistics" -> criminology, sociology, "social science".

BC AD

1000

17th C

1700



The discovery of "social facts" Stability and Variation

Guerry's results were both compelling and startling:

- Rates of crime and suicide remained remarkably invariant over time, yet varied sytematically by region, sex of accused, type of crime, etc.
- In any given French city or department, almost the same number committed suicide, stole, gave birth out of wedlock, etc.

| Year | 1826 | 1827 | 1828 | 1829 | 1830 | Avg |
|---------------------|-------------------------|------|------|------|------|-----|
| Sex All accused (%) | | | | | | |
| Male | 79 | 79 | 78 | 77 | 78 | 78 |
| Female | 21 | 21 | 22 | 23 | 22 | 22 |
| Age | Accused of Theft (%) | | | | | |
| 16–25 | 37 | 35 | 38 | 37 | 37 | 37 |
| 25–25 | 31 | 32 | 30 | 31 | 32 | 31 |
| Crime | Committed in summer (%) | | | | | |
| Indecent assault | | 36 | 36 | 35 | 38 | 36 |
| Assault & battery | | 28 | 27 | 27 | 27 | 28 |

"We are forced to conclude that the facts of the moral order are subject, like those of the physical order to invariable laws." (Guerry, 1833, p14)

Social context of crime in 1820s

What to do about crime?

- Crime a serious concern: Explosive growth in Paris, widespread unemployment, emergence of "dangerous classes"
- Liberal ("philanthrope") view: increase education, better prison conditions, religious instruction, better diet (bread and soup)
- Conservative view: build more prisons, harsher treatment of recidivists
- But: there was very little data!
 - That would soon change

An avalanche of social numbers

- J.B.J. Fourier: Recherches statistique sur la ville de Paris (1821-9)
 - Massive tabulations: births, deaths (by cause), admission to insane asylums (age, sex, affliction)
- Ministry of Justice: Compte generale (1825--)
 - First national compilation of criminal justice data
 - All charges & dispositions, quarterly, 86 departments
- Other sources:
 - Bureau de Longitudes (illegitimate births)
 - Parent-Duchatelet (prostitution); Min. of War (desertions)
- Social issues could now be addressed with DATA

1829: Statistique comparée de l'état de l'instruction...

- First shaded thematic maps of crime data
- First comparative maps of social data
- inversely related
 to crime against property!
- Instruction: → France obscure and France éclairée (Dupin, 1826)
- North of France highest in education, but also in property crime!



1864: Statistique morale de l'Angleterre comparée... Dayenu!

- Proposes to replace simple "moral statistics" (tables) with "analytical statistics"
 - calculation, graphic display
 - ► → general, abstract results
- ▶ 17 large color plates (56 × 39 cm):
 - data for France (1825–1855), England (1834 - 1855)
 - crimes against persons and property decomposed in various ways
 - ► first attempt to delineate multivariate relations among moral variables
- Voluminous data:
 - 85,564 suicide records (1836–1860), classified by motive
 - 226,224 accused of personal crime
 - ▶ numbers, in a line → 1170 meters!

L'ANGLETERRE LA STATISTIQUE MORALE LA FRANCE ande las campas, per c'arterna como ser es por al conteners de campanes en en recordo para Antiga ar es percer el arterna, nel alcance, en estanciat, en , que moduripares el en econ PAN A.-N. GUERRY Carter Street ATLAS PERMIT plantice prette PROSPECTUS PARIS 1.+0. BAILLIERE ET FILS,

STATISTIQUE MORALE

English counties (ranked on each)

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1864: Statistique morale de l'Angleterre comparée... Comparing France and England



Statistique analytique: General causes of crime

Plate XVII: M. Guerry's magnum opus

Goal:

max mi Show multivariate factors -----High pop. associated with distribution of density on crime · Before invention of correlation Crimes (ranked) Curve of neg. association Entries: Codes for factors • Pop: (% Irish, domestics, ...) Curve of pos. • Criminality: (male, young, ...) pe association • Religion (Anglicans, dissenters, ...) murde 10 Y 4 8 X ancm1/ kapbubk dfan Ehwao E Langer

The graphic vision of C. J. Minard



- Marey (1878): "defies the pen of the historian in its brutal eloquence" ٠
- Tufte (1983): "the best statistical graphic ever produced" ٠

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Why Minard?

- Study breadth and depth of his work
 - How related to work in his time?
 - How related to modern statistical graphics?
 - How related to his personal history?



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Visual thinking, visual explanation

1840: Why did the bridge at Bourg-St. Andèol collapse?

Minard's report consisted essentially of this self-explaining diagram.



Visual tools for state planning

- 1830—1860: emergence of modern French state, dawn of globalization
- Trade, commerce, transportation:
 - Where to build railroads, canals?
 - Visualizing changes over time, differences over space
 - $\blacksquare \rightarrow$ Flow maps and other graphical innovations

Flow maps as visual tools

Transport of passengers on the principal railroads in Europe in 1862



Effect of US civil war on cotton trade





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Where to build a new post office?(1867)



Center of gravity of pop. density

The March Re-Visited (1869)



Galton's visual discoveries-Bivariate normal correlation surface (1886)

Table 9.1 One of Galton's correlation tables

| Height of the mid- | Height of the adult child | | | | | | | | | | | | | |
|---------------------|---------------------------|------|------|------|------|------|------|------|------|------|------|------|------|-------|
| parent in inches | <61.7 | 62.2 | 63.2 | 64.2 | 65.2 | 66.2 | 67.2 | 68.2 | 69.2 | 70.2 | 71.2 | 72.2 | 73.2 | >73.7 |
| >73.0 | | | | _ | _ | | _ | _ | _ | _ | _ | 1 | 3 | _ |
| 72.5 | | _ | | | | - | _ | 1 | 2 | 1 | 2 | 7 | 2 | 4 |
| 71.5 | | | | - | 1 | 3 | 4 | 3 | 5 | 10 | 4 | 9 | 2 | 2 |
| 70.5 | 1 | _ | 1 | _ | 1 | 1 | 3 | 12 | 18 | 14 | 7 | 4 | 3 | 3 |
| 69.5 | | _ | 1 | 16 | 4 | 17 | 27 | 20 | 33 | 25 | 20 | 11 | 4 | 5 |
| 68.5 | 1 | _ | 7 | 11 | 16 | 25 | 31 | 34 | 48 | 21 | 18 | 4 | 3 | - |
| 67.5 | _ | 3 | 5 | 14 | 15 | 36 | 38 | 28 | 38 | 19 | 11 | 4 | — | |
| 66.5 | _ | 3 | 3 | 5 | 2 | 17 | 17 | 14 | 13 | 4 | | | — | - |
| 65.5 | 1 | - | 9 | 5 | 7 | 11 | 11 | 7 | 7 | 5 | 2 | 1 | — | — |
| 64.5 | 1 | 1 | 4 | 4 | 1 | 5 | 5 | | 2 | | — | | — | — |
| <64.0 | 1 | _ | 2 | 4 | 1 | 2 | 2 | 1 | 1 | | _ | — | - | — |
| Totals | 5 | 7 | 32 | 59 | 48 | 117 | 138 | 120 | 167 | 99 | 64 | 41 | 17 | 14 |
| Medians | _ | _ | 66.3 | 67.8 | 67.9 | 67.7 | 67.9 | 68.3 | 68.5 | 69.0 | 69.0 | 70.0 | — | _ |

Source: Galton (1886), p. 68.

Visual smoothing \rightarrow Insight

Table 9.1 One of Galton's correlation tables



Visual insight \rightarrow Theory



... that Galton should have evolved all this ... is to my mind one of the most noteworthy scientific discoveries arising from analysis of pure observation (Pearson 1920, p37)



Galton (1886, PI X): Smoothed contours of heights of parents and children 30

Galton's discovery of weather patterns-

Perhaps the most notable purely graphic discovery ever!

METEOROGRAPHICA,

METHODS OF MAPPING THE WEATHER;

ILLUSTRATED BY UPWARDS OF 600 PRINTED AND LITHOGRAPHED DIAGRAMS REFERENCE. TO

THE WEATHER OF A LARGE PART OF EUROPE,

During the Month of December 1861.

By FRANCIS GALTON, F.R.S.

(Galton, 1863)

Method: All weather stations across Europe asked to record data 3x/day for all of Dec., 1861

Data: recordings of barometric pressure, wind dir/speed, rain, temp., cloud: 3x/day, 50 weather stations in Europe.

Graphic analysis: 3x31=93 maps, each with multivariate glyphs showing all variables

Visual ideas:

Iconic symbols

Multivariate glyphs (stamps!)



Visual abstraction \rightarrow Patterns

How to see patterns of geographical variation over time?

- · Iconic symbols on a geographical grid
- · "Small multiples:" separate graphs laid out for direct comparison



Visual abstraction \rightarrow Patterns

What varies with what, over time and space?

• mini, abstract maps: vars x TOD

· iso-contours, shading to show equivalence

arrows to show wind direction





Data for Dec 5, 1861

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The large picture \rightarrow Insight

Pattern:

Low pressure (black) in early Dec. \rightarrow CCW wind High pressure (red) in late Dec. \rightarrow CW wind

Graphic: 3x3x31 grid, mapping {pressure, wind/ rain, temperature} x {AM, 12, PM} x day {1:31}

(try this with your software!)



Visual insight \rightarrow Theory

Visual insight from 93 (3x31) high-D graphs:

· Changes in wind dir w/ pressure over time • \rightarrow Winds revolve inwardly

(CCW) in low pressure areasas in a cvclone:

• → revolve outwardly (CW) in high pressure areas- "anticyclone"

Theory:

· Explained by Dove's 'Law of Gyration'

 Prediction: reversed pattern (CW/CCW) in southern hemisphere - confirmed!

Theory → Practice

The first modern weather map, *London Times*, Apr. 1, 1875

Galton did for weathermen what Kepler did for Tycho Brahe. This is no small accomplishment. (Wainer 2005)

The dotted lines indicate the gradations of barometric pressure The variations of the temperature are marked by figures, the state of the sea and sky by descriptive words, and the direction of the wind by arrows-barbed and feathered according to its force. O denotes alm.

Statistical albums: Data \rightarrow practice & Graphical excellence

- Collection of gov't statistics on pop., trade, moral & political issues widespread in Europe & US, starting ~ 1820
- Statistical albums ~ 1870—1910
 - France: Albums de Statistique Graphique
 - Gemany: local albums (Berlin, Frankfurt, etc.)
 - Switzerland: Atlas graphique de la Suisse
 - USA: Census atlases: 1870/80/90

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Album de statistique graphique

• The pinnacle of the Golden Age

• 18 volumes published 1879-1899

Changes in the population of France from 1801—1881, by department (Album, 1881)

Album de statistique graphique

Gross receipts in theaters in Paris, 1848—1889, related to cultural events (Album, 1889)

Follies Bergère

Atlas graphique de la Suisse (1897, 1914)

Atlas graphique de la Suisse (1897, 1914)

Causes of death, 1890—1894, color linking (Atlas, 1897)

Atlas graphique de la Suisse (1897, 1914)

Referendum on development of railroads in 1896 - bipolar color scale

Where are we today?

- Analysis graphs for exploration and model diagnosis (linear models)
- Graphical methods for categorical data & frequency tables (generalized linear models)
- Ease of use? Interactive data graphics?
- Cognitive interfaces for models and graphics?

Graphical methods for linear models

| | | Classical linear models | Generalized linear models | | | |
|--------|------------|--|--|--|--|--|
| les | 1 | LM family: $E(\mathbf{y})=\mathbf{X}\beta$, $V(\mathbf{y} \mathbf{X})=\sigma^{2}\mathbf{I}$ | GLM: E(y)=g ⁻¹ (X β), V=V[g ⁻¹ (X β)] | | | |
| riab | | ANOVA, regression, | poisson, logistic, loglinear, | | | |
| se vai | Å | Many graphical methods: effect plots, spread-leverage, influence, | Some graphical methods: mosaic plots, 4fold plots, diagnostic plots, | | | |
| Ö | 2+ | MLM: E(Y) =X β, V(Y X)=I⊗Σ | MGLM: ??? | | | |
| est | | MANOVA, MMReg, | | | | |
| # ot I | - 1 | Graphical methods: ??? | Graphical methods: ??? | | | |

Model diagnosis: Influence in regression

Multiple regression model: prestige ~ income + education

model residual

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influence ~ residual x

Model diagnosis: regression quartet

Graphical methods for GLMs

| | | Classical linear models | Generalized linear models |
|-----------|----|--|--|
| les | 1 | LM family: $E(\mathbf{y})=\mathbf{X}\beta$, $V(\mathbf{y} \mathbf{X})=\sigma^{2}\mathbf{I}$ | GLM: $E(\mathbf{y})=g^{-1}(\mathbf{X}\beta), V=V[g^{-1}(\mathbf{X}\beta)]$ |
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| d of | | MANOVA, MMReg, | |
| - IO # | | Graphical methods: ??? | Graphical methods: ??? |

Visualizing categorical data: mosaic plots

Model: loglin(~ Hair + Eye)

A contingency table can be visualized by tiles whose area ~ cell frequency.

Shading: ~ Pearson residual,

$d_{ij} = (O_{ij} - E_{ij}) / \sqrt{E_{ij}}$

4.00 Color:

7.05

-2.00

--4.00

--5.85

Interp: + association (dark hair, dark eyes), (light hair, light eyes)

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N-way tables

Model: loglin(~ Hair + Eye + Sex)

3+ way tables: split each tile ~ conditional proportions of the next variable.

- Now, there are several different models that can be fit.
- Mutual independence: [H][E][S] \rightarrow all vars unassociated
- Residuals: show associations not acct'd for by the model

N-way tables

The model of joint independence, [HE][S] allows Hair. Eve color association, but \rightarrow [HE] assoc. is independent of Sex.

This model obviously fits much better, except for blue-eved blonds, where females are more prevalent than the model allows.

Mosaic displays: visual assessment of model fit:

Better model \rightarrow "cleans the mosaic"

Cognitive interfaces for data exploration & model-fitting

- "Dumb" vs. "Smart" data tables: variables assigned default roles (factor, covariate, response, label)
- Model syntax, e.g., loglin(~ Hair+Eye+Sex) vs. modelbuilding widgets & GUIs
- Begging for graphs vs. getting them (semi-)automatically
- Model history: easily compare, modify or explore multiple models for the same data
- Dynamic, interactive graphics ٠
 - Multiple, linked views: data table, 2D graphs, 3D plots
 - Selection: subset or highlight all views for a given selection
 - Projection & low-D views of hi-D data

JMP: Model summary = graphs + numbers

JMP: Model summary = graphs + numbers

Summarizes 15 years of research

• Visual interfaces for statistical analysis & dynamic graphics

• Testbed: ViSta http://forrest.psych.unc.edu/research/

• Spreadplots: graphic analog of spreadsheet

• Work maps: visual GUI for path(s) of analysis

• Guide maps: visually guide novices thru typical analysis steps

ViSta: regression spreadplots

ViSta: loglin spreadplots

The future of statistical graphics?

- New visualizations for statistical methods
 - Closer integration of analysis (summarization) and graphics (exposure)
 - E.g., HE plots for MLMs
- Public data, public graphics
 - Worldmapper the world in cartograms
 - Facebook for data & graphs?
 - Gapminder analyzing trends and relations

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Graphical excellence

Graphical methods for MLMs

| - | | | | | |
|----------|--|--|--|--|--|
| | Classical linear models | Generalized linear models | | | |
| 1 | LM family: $E(\mathbf{y})=\mathbf{X}\beta$, $V(\mathbf{y} \mathbf{X})=\sigma^2$ | GLM: $E(\mathbf{y})=g^{-1}(\mathbf{X}\beta), V=V[g^{-1}(\mathbf{X}\beta)]$ | | | |
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| 2+ | MLM: E(Y) =X β, V(Y X)= I⊗Σ | MGLM: ??? | | | |
| <u>}</u> | MANOVA, MMReg, | | | | |
| | Graphical methods: ??? | Graphical methods: ??? | | | |

HE plots for MANOVA, MMReg

HE plots provide a way to visualize hypothesis tests in MANOVA and multivariate multiple regression, using data ellipses for fitted (H) and residual (E) co-variances.

Graphic ideas: (a) Data ellipses summarize H & E (co)variation; (b) Scale H ellipse so it projects outside E ellipse *iff* effect is significant (Roy test)

HE plot matrices

HE plots in a scatterplot matrix show effects for all pairs of responses.

For the iris data, the Species means are highly correlated on all variables except Sepal length.

HE plots: 2-way MANOVA

Plastic film data: 2x2 MANOVA

(gloss, opacity, tear) ~ rate*additive

MANOVA tests show that both main effects are significant:

HE plot shows the nature of these effects, e.g.,

high rate: ↑tear, ↑opacity, ↓gloss

1 df tests: H ellipsoid collapses to a line 62

HE plots: Multivariate regression

Rohwer data: Cognitive ability and PA tests: n=37, Low SES group

(SAT, PPVT, Raven) ~ n + s + ns + na + ss

• Only one predictor, NA, is (barely) significant

• Yet, overall multivariate test: H₀: **B** = **0** is highly so!

Public data, public graphics

- Worldmapper the world in cartograms
- ManyEyes, Swivel Facebook for data & graphs
- Gapminder analyzing trends and relations
- Online communities?
- Visualization tools: availability & accessibility

Worldmapper: The world in cartograms

How to visualize social, economic, disease, ... data for geographic units? worldmapper.com : cartograms: area ~ variable of interest (350+ maps)

Worldmapper: The world in cartograms

Worldmapper: The world in cartograms

Worldmapper: The world in cartograms

"I have come to the conclusion that HIV/AIDS is not entirely about death. People die and teill continue to die for one reason or the other. AIDS is also about the living." KII2a NgonZ. 2004 Wm270 Mgr 20 KiI2a NgonZ. 2004

Worldmapper: The world in cartograms

Swivel: Facebook for data & graphs

http://www.swivel.com/ : upload & explore your data

ManyEyes: Social data analysis & visualization

http://services.alphaworks.ibm.com/manyeyes/app

Vineyards: 284.5

Gapminder: Exploring trends in world health

Gapminder: Exploring trends in world health

Gapminder: visualizing trends and relations

Online communities

Map by Randall Munroe of online communities. Area ~ # users

(Berners-Lee projection)

What else do we need? Visualization Tools: Availability & Accessibility

apps

Practical power = Statistical power x Probability of use (J.W. Tukey)

Summary & conclusions

- Past history teaches us that—
 - Statistical graphics always has a purpose: tell a story, inform a decision
 - Statistical graphics is hard work, but can have both beauty & truth
 - Advances require: data, technology & visual thinking

Summary & conclusions

- Present history suggests that—
 - Generalized models → generalized graphics
 - Consumers & producers: different strokes for different folks
 - Most want graphical toasters: data in, picture out (but: what picture(s)?)
 - Some want complete control of graphic details
 - · Graphic developers want it all: freedom to invent

Summary & conclusions

- The future of statistical graphics?
 - New visualizations for statistical methods
 - Open source, open data, online communities
 - Leveraging new technologies for visualization, analysis & data → {insight, practice}