

Chapter 2

Working with categorical data

{ch:working}

Creating and manipulating categorical data sets requires some skills and techniques in R beyond those ordinarily used for quantitative data. This chapter illustrates these for the main formats for categorical data: case form, frequency form and table form.

Categorical data can be represented as data sets in various formats: case form, frequency form, and table form. This chapter describes and illustrates the skills and techniques in R needed to input, create and manipulate R data objects to represent categorical data, and convert these from one form to another for the purposes of statistical analysis and visualization which are the subject of the remainder of the book.

As mentioned earlier, this book assumes that you have at least a basic knowledge of the R language and environment, including interacting with the R console (Rgui for Windows, R.app for Mac OS X) or some other graphical user interface (e.g., R Studio), loading and using R functions in packages (e.g., `library(vcd)`) getting help for these from R (e.g., `help(matrix)`), etc. This chapter is therefore devoted to covering those topics beyond such basic skills needed in the book.¹

2.1 Working with R data: vectors, matrices, arrays and data frames

{sec:Rdata}

R has a wide variety of data structures for storing, manipulating and calculating with data. Among these, vectors, matrices, arrays and data frames are most important for the material in this book.

In R, a *vector* is a collection of values, like numbers, character strings, logicals (`TRUE`, `FALSE`) or dates, and often correspond to a variable in some analysis. Matrices are rectangular arrays like a traditional table, composed of vectors in their columns or rows. Arrays add additional dimensions, so that, for example, a 3-way table can be represented as composed of rows, columns and layers. An important consideration is that the values in vectors, matrices and arrays must all be of the same *mode*, e.g., numbers or character strings. A *data frame* is a rectangular table, like a traditional data set in other statistical environments, and composed of rows and columns like a matrix, but allowing variables (columns) of different types. These data structures and the types

¹Some excellent introductory treatments of R are: Fox and Weisberg (2011, Chapter 2), ... Tom Short's *R Reference Card*, <http://cran.us.r-project.org/doc/contrib/Short-refcard.pdf> is a handy 4-page summary of the main functions. The web sites Quick-R <http://www.statmethods.net/> and Cookbook for R <http://www.cookbook-r.com/> provide very helpful examples, organized by topics and tasks.

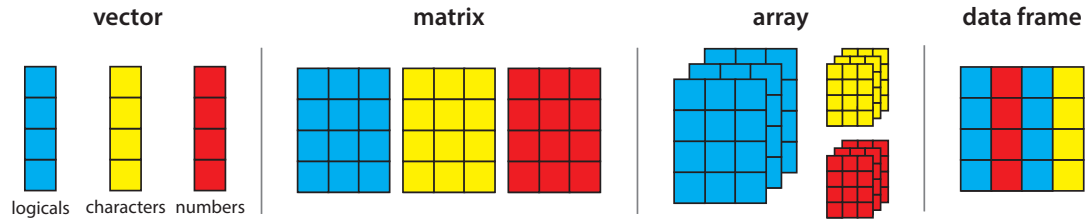


Figure 2.1: Principal data structures and data types in R. Colors represent different data types: numeric, character, logical.

{fig:datatypes}

of data they can contain are illustrated in Figure 2.1. A more general data structure is a *list*, a generic vector which can contain any other types of objects.

2.1.1 Vectors

The simplest data structure in R is a *vector*, a one-dimensional collection of elements of the same type. An easy way to create a vector is with the `c()`, which combines its arguments. The following examples create and print vectors of length 4, containing numbers, character strings and logical values respectively:

```
c(17, 20, 15, 40)

## [1] 17 20 15 40

c("female", "male", "female", "male")

## [1] "female" "male" "female" "male"

c(TRUE, TRUE, FALSE, FALSE)

## [1] TRUE TRUE FALSE FALSE
```

To store these values in variables, R uses the assignment operator (`<-`) or equals sign (`=`). This creates a variable named on the left-hand side. An assignment doesn't print the result, but a bare expression does, so you can assign and print by surrounding the assignment with `()`.

```
count <- c(17, 20, 15, 40)           # assign
count                               # print

## [1] 17 20 15 40

(sex <- c("female", "male", "female", "male")) # both

## [1] "female" "male" "female" "male"

(passed <- c(TRUE, TRUE, FALSE, FALSE))

## [1] TRUE TRUE FALSE FALSE
```

Other useful functions for creating vectors are:

- The `:` operator for generating consecutive integer sequences, e.g., `1:10` gives the integers 1 to 10. The `seq()` function is more general, taking the forms `seq(from, to)`, `seq(from, to, by=)`, and `seq(from, to, length=)` where the optional argument `by` specifies the interval between adjacent values and `length` gives the desired length of the result.
- The `rep()` function generates repeated sequences, replicating its first argument (which may be a vector) a given number of times, to a given length or each a given multiple.

```
seq(10, 100, by=10)      # give interval
## [1] 10 20 30 40 50 60 70 80 90 100

seq(0, 1, length=11)    # give length
## [1] 0.0 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9 1.0

(sex <- rep(c("female", "male"), times=2))
## [1] "female" "male" "female" "male"

(sex <- rep(c("female", "male"), length.out=4)) # same
## [1] "female" "male" "female" "male"

(passed <- rep(c(TRUE, FALSE), each=2))
## [1] TRUE TRUE FALSE FALSE
```

2.1.2 Matrices

A *matrix* is a two-dimensional array of elements of the same type composed in a rectangular array of rows and columns. Matrices can be created by the function `matrix(values, nrow, ncol)`, which takes the reshapes the elements in the first argument (`values`) to a matrix with `nrow` rows and `ncol` columns. By default, the elements are filled in columnwise, unless the optional argument `byrow=TRUE` is given.

```
(matA <- matrix(1:8, nrow=2, ncol=4))
##      [,1] [,2] [,3] [,4]
## [1,]  1   3   5   7
## [2,]  2   4   6   8

(matB <- matrix(1:8, nrow=2, ncol=4, byrow=TRUE))
##      [,1] [,2] [,3] [,4]
## [1,]  1   2   3   4
## [2,]  5   6   7   8

(matC <- matrix(1:4, nrow=2, ncol=4))
##      [,1] [,2] [,3] [,4]
## [1,]  1   3   1   3
## [2,]  2   4   2   4
```

The last example illustrates that the values in the first argument are recycled as necessary to fill the given number of rows and columns.

All matrices have a `dim` attribute, a vector of length two giving the number of rows and columns, retrieved with the function `dim()`. Labels for the rows and columns can be assigned using `dimnames()`,² which takes a list of two vectors for the row names and column names respectively. To see the structure of a matrix (or any other R object) and its attributes, I frequently use the `str()` function, as shown in the example below.

```
dim(matA)

## [1] 2 4

str(matA)

## int [1:2, 1:4] 1 2 3 4 5 6 7 8

dimnames(matA) <- list(c("M", "F"), LETTERS[1:4])
matA

##   A B C D
## M 1 3 5 7
## F 2 4 6 8

str(matA)

## int [1:2, 1:4] 1 2 3 4 5 6 7 8
## - attr(*, "dimnames")=List of 2
## ..$ : chr [1:2] "M" "F"
## ..$ : chr [1:4] "A" "B" "C" "D"
```

Additionally, names for the row and column *variables* themselves can also be assigned in the `dimnames` call by giving each dimension vector a name.

```
dimnames(matA) <- list(sex=c("M", "F"), group=LETTERS[1:4])
matA

##   group
## sex A B C D
## M 1 3 5 7
## F 2 4 6 8

str(matA)

## int [1:2, 1:4] 1 2 3 4 5 6 7 8
## - attr(*, "dimnames")=List of 2
## ..$ sex : chr [1:2] "M" "F"
## ..$ group: chr [1:4] "A" "B" "C" "D"
```

Matrices can also be created or enlarged by “binding” vectors or matrices together by rows or columns:

- `rbind(a, b, c)` creates a matrix with the vectors `a`, `b` and `c` as its rows, recycling the elements as necessary to the length of the longest one.

²The `dimnames` can also be specified as an optional argument to `matrix()`.

- `cbind(a, b, c)` creates a matrix with the vectors `a`, `b` and `c` as its columns.
- `rbind(mat, a, b, ...)` and `cbind(mat, a, b, ...)` add additional rows (columns) to a matrix `mat`, recycling or subsetting the elements in the vectors to conform with the size of the matrix.

```
rbind(matA, c(10,20))
```

```
##      A B C D
## M   1 3 5 7
## F   2 4 6 8
##      10 20 10 20
```

```
cbind(matA, c(10,20))
```

```
##      A B C D
## M   1 3 5 7 10
## F   2 4 6 8 20
```

2.1.3 Arrays

Higher-dimensional arrays are less frequently encountered in traditional data analysis, but they are of great use for categorical data, where frequency tables of three or more variables can be naturally represented as arrays, with one dimension for each table variable.

The function `array(values, dim)` takes the elements in `values` and reshapes these into an array whose dimensions are given in the vector `dim`. The number of dimensions is the length of `dim`. As with matrices, the elements are filled in with the first dimension (rows) varying most rapidly, then by the second dimension (columns) and so on for all further dimensions, which can be considered as layers. A matrix is just the special case of an array with two dimensions.

```
(arrayA <- array(1:16, dim=c(2, 4, 2)))      # 2 rows, 4 columns, 2 layers
```

```
##      , , 1
##
##      [,1] [,2] [,3] [,4]
## [1,]    1    3    5    7
## [2,]    2    4    6    8
##
```

```
##      , , 2
##
##      [,1] [,2] [,3] [,4]
## [1,]    9   11   13   15
## [2,]   10   12   14   16
```

```
str(arrayA)
```

```
## int [1:2, 1:4, 1:2] 1 2 3 4 5 6 7 8 9 10 ...
```

```
(arrayB <- array(1:16, dim=c(2, 8)))      # 2 rows, 8 columns
```

```
##      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
## [1,]    1    3    5    7    9   11   13   15
## [2,]    2    4    6    8   10   12   14   16
```

```
str(arrayB)
```

```
## int [1:2, 1:8] 1 2 3 4 5 6 7 8 9 10 ...
```

In the same way that we can assign labels to the rows, columns and variables in matrices, we can assign these attributes to `dimnames(arrayA)`, or include this information in a `dimnames=` argument to `array()`.

```
dimnames(arrayA) <- list(sex=c("M", "F"),
                        group=letters[1:4],
                        time=c("Pre", "Post"))

arrayA

## , , time = Pre
##
##   group
## sex a b c d
##  M 1 3 5 7
##  F 2 4 6 8
##
## , , time = Post
##
##   group
## sex  a  b  c  d
##  M  9 11 13 15
##  F 10 12 14 16

str(arrayA)

## int [1:2, 1:4, 1:2] 1 2 3 4 5 6 7 8 9 10 ...
## - attr(*, "dimnames")=List of 3
## ..$ sex : chr [1:2] "M" "F"
## ..$ group: chr [1:4] "a" "b" "c" "d"
## ..$ time : chr [1:2] "Pre" "Post"
```

Arrays in R can contain any single type of elements— numbers, character strings, logicals. R also has a variety of functions (e.g., `table()`, `xtabs()`) for creating and manipulating "table" objects, which are specialized forms of matrices and arrays containing integer frequencies in a contingency table. These are discussed in more detail below (Section 2.4).

2.1.4 data frames

{sec:data-frames}

Data frames are the most commonly used form of data in R and more general than matrices in that they can contain columns of different types. For statistical modeling, data frames play a special role, in that many modeling functions are designed to take a data frame as a `data=` argument, and then find the variables mentioned within that data frame. Another distinguishing feature is that discrete variables (columns) like character strings ("M", "F") or integers (1, 2, 3) in data frames can be represented as *factors*, which simplifies many statistical and graphical methods.

A data frame can be created using keyboard input with the `data.frame()` function, applied to a list of objects, `data.frame(a, b, c, ...)`, each of which can be a vector, matrix or another data frame, but typically all containing the same number of rows. This works roughly like `cbind()`, collecting the arguments as columns in the result.

The following example generates `n=100` random observations on three discrete factor variables, `A`, `B`, `sex`, and a numeric variable, `age`. As constructed, all of these are statistically independent, since none depends on any of the others. The function `sample()` is used here to

generate n random samples from the first argument allowing replacement (`rep=TRUE`). Finally, all four variables are combined into the data frame `mydata`.

```
set.seed(12345) # reproducibility
n=100
A <- factor(sample(c("a1", "a2"), n, rep=TRUE))
B <- factor(sample(c("b1", "b2"), n, rep=TRUE))
sex <- factor(sample(c("M", "F"), n, rep=TRUE))
age <- round(rnorm(n, mean=30, sd=5))
mydata <- data.frame(A, B, sex, age)
head(mydata, 5)

##      A  B sex age
## 1 a2 b1  F  22
## 2 a2 b2  F  33
## 3 a2 b2  M  31
## 4 a2 b2  F  26
## 5 a1 b2  F  29

str(mydata)

## 'data.frame': 100 obs. of  4 variables:
##  $ A  : Factor w/ 2 levels "a1","a2": 2 2 2 2 1 1 1 2 2 2 ...
##  $ B  : Factor w/ 2 levels "b1","b2": 1 2 2 2 2 2 2 2 1 1 ...
##  $ sex: Factor w/ 2 levels "F","M": 1 1 2 1 1 1 2 2 1 1 ...
##  $ age: num  22 33 31 26 29 29 38 28 30 27 ...
```

For real data sets, it is usually most convenient to read these into R from external files, and this is easiest using plain text (ASCII) files with one line per observation and fields separated by commas (or tabs), and with a first header line giving the variable names— called *comma-separated* or CSV format. If your data is in the form of Excel, SAS, SPSS or other file format, you can almost always export that data to CSV format first.³

The function `read.table()` has many options to control the details of how the data are read and converted to variables in the data frame. Among these some important options are:

`header` indicates whether the first line contains variable names. The default is `FALSE` unless the first line contains one fewer field than the number of columns;

`sep` (default: " " meaning white space, i.e., one or more spaces, tabs or newlines) specifies the separator character between fields;

`stringsAsFactors` (default: `TRUE`) determines whether character string variables should be converted to factors;

`na.strings` (default: "NA") one or more strings which are interpreted as missing data values (NA);

For delimited files, `read.csv()` and `read.delim()` are convenient wrappers to `read.table()`, with default values `sep=","` and `sep="\r"` respectively, and `header=TRUE`.

{ex:ch2-arth-csv}

EXAMPLE 2.1: Arthritis treatment

³The foreign package contains specialized functions to *directly* read data stored by Minitab, SAS, SPSS, Stata, Systat and other software. There are also a number of packages for reading (and writing) Excel spreadsheets directly (`gdata`, `XLConnect`, `xlsx`). The R manual, *R Data Import/Export* covers many other variations, including data in relational data bases.

The file `Arthritis.csv` contains data in CSV format from Koch and Edwards (1988), representing a double-blind clinical trial investigating a new treatment for rheumatoid arthritis with 84 patients. The first (“header”) line gives the variable names. Some of the lines in the file are shown below, with . . . representing omitted lines:

```
ID, Treatment, Sex, Age, Improved
57, Treated, Male, 27, Some
46, Treated, Male, 29, None
77, Treated, Male, 30, None
17, Treated, Male, 32, Marked
...
42, Placebo, Female, 66, None
15, Placebo, Female, 66, Some
71, Placebo, Female, 68, Some
1, Placebo, Female, 74, Marked
```

We read this into R using `read.csv()` as shown below, using all the default options:

```
Arthritis <- read.csv("ch02/Arthritis.csv")
str(Arthritis)

## 'data.frame': 84 obs. of 5 variables:
## $ ID : int 57 46 77 17 36 23 75 39 33 55 ...
## $ Treatment: Factor w/ 2 levels "Placebo","Treated": 2 2 2 2 2 2 2 2 2 2 ...
## $ Sex : Factor w/ 2 levels "Female","Male": 2 2 2 2 2 2 2 2 2 2 ...
## $ Age : int 27 29 30 32 46 58 59 59 63 63 ...
## $ Improved : Factor w/ 3 levels "Marked","None",...: 3 2 2 1 1 1 2 1 2 2 ...
```

Note that the character variables *Treatment*, *Sex* and *Improved* were converted to factors, and the levels of those variables were ordered *alphabetically*. This often doesn’t matter much for binary variables, but here, the response variable, *Improved* has levels that should be considered *ordered*, as "None", "Some", "Marked". We can correct this here by re-assigning `Arthritis$Improved` using `ordered()`. The topic of re-ordering variables and levels in categorical data is considered in more detail in Section 2.3.

```
levels(Arthritis$Improved)

## [1] "Marked" "None" "Some"

Arthritis$Improved <- ordered(Arthritis$Improved,
                             levels=c("None", "Some", "Marked"))
```

△

2.2 Forms of categorical data: case form, frequency form and table form

{sec:forms}

As we saw in Chapter 1, categorical data can be represented as ordinary data sets in case form, but the discrete nature of factors or stratifying variables allows the same information to be represented more compactly in summarized form with a frequency variable for each cell of factor combinations, or in tables. Consequently, we sometimes find data created or presented in one form (e.g., a spreadsheet data set, a two-way table of frequencies) and want to input that into R. Once we have the data in R, it is often necessary to manipulate the data into some other form for the purposes of statistical analysis, visualizing results and our own presentation. It is useful

to understand the three main forms of categorical data in R and how to work with them for our purposes.

2.2.1 Case form

Categorical data in case form are simply data frames, with one or more discrete classifying variables or response variables, most conveniently represented as factors or ordered factors. In case form, the data set can also contain numeric variables (covariates or other response variables), that cannot be accommodated in other forms.

As with any data frame, X , you can access or compute with its attributes using `nrow(X)` for the number of observations, `ncol(X)` for the number of variables, `names(X)` or `colnames(X)` for the variable names and so forth.

{ex:ch2-arth}

EXAMPLE 2.2: Arthritis treatment

The `Arthritis` data is available in case form in the `vcd` package. There are two explanatory factors: `Treatment` and `Sex`. `Age` is a numeric covariate, and `Improved` is the response—an ordered factor, with levels "None" < "Some" < "Marked". Excluding `Age`, we would have a $2 \times 2 \times 3$ contingency table for `Treatment`, `Sex` and `Improved`.

```
data(Arthritis, package="vcd") # load the data
names(Arthritis)              # show the variables

## [1] "ID"          "Treatment" "Sex"        "Age"        "Improved"

str(Arthritis)                # show the structure

## 'data.frame': 84 obs. of 5 variables:
## $ ID      : int  57 46 77 17 36 23 75 39 33 55 ...
## $ Treatment: Factor w/ 2 levels "Placebo","Treated": 2 2 2 2 2 2 2 2 2 ...
## $ Sex      : Factor w/ 2 levels "Female","Male": 2 2 2 2 2 2 2 2 2 ...
## $ Age      : int  27 29 30 32 46 58 59 59 63 63 ...
## $ Improved : Ord.factor w/ 3 levels "None"<"Some"<"..: 2 1 1 3 3 3 1 3 1 1 ...

head(Arthritis,5)            # first 5 observations, same as Arthritis[1:5,]

##   ID Treatment Sex Age Improved
## 1  57   Treated Male  27     Some
## 2  46   Treated Male  29     None
## 3  77   Treated Male  30     None
## 4  17   Treated Male  32    Marked
## 5  36   Treated Male  46    Marked
```

△

2.2.2 Frequency form

Data in frequency form is also a data frame, containing one or more discrete factor variables and a frequency variable (often called `Freq` or `count`) representing the number of basic observations in that cell.

This is an alternative representation of a table form data set considered below. In frequency form, the number of cells in the equivalent table is `nrow(X)`, and the total number of observations is the sum of the frequency variable, `sum(X$Freq)`, `sum(X[, "Freq"])` or similar expression.

{ex:ch2-GSS}

EXAMPLE 2.3: General social survey

For small frequency tables, it is often convenient to enter them in frequency form using `expand.grid()` for the factors and `c()` to list the counts in a vector. The example below, from Agresti (2002) gives results for the 1991 General Social Survey, with respondents classified by sex and party identification. As a table, the data look like this:

	party		
sex	dem	indep	rep
female	279	73	225
male	165	47	191

We use `expand.grid()` to create a 6×2 matrix containing the combinations of `sex` and `party` with the levels for `sex` given first, so that this varies most rapidly. Then, input the frequencies in the table by columns from left to right, and combine these two results with `data.frame()`.

```
# Agresti (2002), table 3.11, p. 106
GSS <- data.frame(
  expand.grid(sex=c("female", "male"),
             party=c("dem", "indep", "rep")),
  count=c(279, 165, 73, 47, 225, 191))
GSS

##      sex party count
## 1 female  dem   279
## 2  male   dem   165
## 3 female indep    73
## 4  male  indep    47
## 5 female  rep   225
## 6  male   rep   191

names(GSS)

## [1] "sex" "party" "count"

str(GSS)

## 'data.frame': 6 obs. of 3 variables:
## $ sex : Factor w/ 2 levels "female","male": 1 2 1 2 1 2
## $ party: Factor w/ 3 levels "dem","indep",..: 1 1 2 2 3 3
## $ count: num 279 165 73 47 225 191

sum(GSS$count)

## [1] 980
```

The last line above shows that there are 980 cases represented in the frequency table. \triangle

2.2.3 Table form

Table form data is represented as a matrix, array or table object whose elements are the frequencies in an n -way table. The number of dimensions of the table is the length, `length(dim(X))`, of its `dim` (or `dimnames`) attribute, and the sizes of the dimensions in the table are the elements

of `dim(X)`. The total number of observations represented is the sum of all the frequencies, `sum(X)`.

ex:ch2-hec}

EXAMPLE 2.4: Hair color and eye color

A classic data set on frequencies of hair color, eye color and sex is given in table form in `HairEyeColor` in the `VCD` package, reporting the frequencies of these categories for 592 students in a statistics course.

```
data(HairEyeColor, package="datasets") # load the data
str(HairEyeColor) # show the structure

## table [1:4, 1:4, 1:2] 32 53 10 3 11 50 10 30 10 25 ...
## - attr(*, "dimnames")=List of 3
## ..$ Hair: chr [1:4] "Black" "Brown" "Red" "Blond"
## ..$ Eye : chr [1:4] "Brown" "Blue" "Hazel" "Green"
## ..$ Sex : chr [1:2] "Male" "Female"

dim(HairEyeColor) # table dimension sizes

## [1] 4 4 2

dimnames(HairEyeColor) # variable and level names

## $Hair
## [1] "Black" "Brown" "Red" "Blond"
##
## $Eye
## [1] "Brown" "Blue" "Hazel" "Green"
##
## $Sex
## [1] "Male" "Female"

sum(HairEyeColor) # number of cases

## [1] 592
```

Three-way (and higher-way) tables can be printed in a more convenient form using `strutable()` and `ftable()` as described below in Section 2.5. △

Tables are often created from raw data in case form or frequency form using the functions `table()` and `xtabs()` described in Section 2.4. For smallish frequency tables that are already in tabular form, you can enter the frequencies in a matrix, and then assign `dimnames` and other attributes.

To illustrate, we create the GSS data as a table below, entering the values in the table by rows (`byrow=TRUE`), as they appear in printed form.

```
GSS.tab <- matrix(c(279, 73, 225,
                  165, 47, 191), nrow=2, ncol=3, byrow=TRUE)
dimnames(GSS.tab) <- list(sex=c("female", "male"),
                        party=c("dem", "indep", "rep"))
GSS.tab

##           party
```

```
## sex      dem indep rep
## female 279   73 225
## male   165   47 191
```

`GSS.tab` is a matrix, not an object of class `"table"`, and some functions are happier with tables than matrices.⁴ You can coerce it to a table with `as.table()`,

```
GSS.tab <- as.table(GSS.tab)
str(GSS.tab)

## table [1:2, 1:3] 279 165 73 47 225 191
## - attr(*, "dimnames")=List of 2
## ..$ sex : chr [1:2] "female" "male"
## ..$ party: chr [1:3] "dem" "indep" "rep"
```

```
{ex:jobsat1}
```

EXAMPLE 2.5: Job satisfaction

Here is another similar example, entering data on job satisfaction classified by income and level of satisfaction from a 4×4 table given by Agresti (2002, Table 2.8, p. 57).

```
## A 4 x 4 table Agresti (2002, Table 2.8, p. 57) Job Satisfaction
JobSat <- matrix(c(1, 2, 1, 0,
                  3, 3, 6, 1,
                  10, 10, 14, 9,
                  6, 7, 12, 11), 4, 4)
dimnames(JobSat) = list(income=c("< 15k", "15-25k", "25-40k", "> 40k"),
                       satisfaction=c("VeryD", "LittleD", "ModerateS", "VeryS"))
JobSat <- as.table(JobSat)
JobSat

##           satisfaction
## income  VeryD LittleD ModerateS VeryS
## < 15k   1         3         10      6
## 15-25k  2         3         10      7
## 25-40k  1         6         14     12
## > 40k   0         1          9     11
```

△

2.3 Ordered factors and reordered tables

```
{sec:ordered}
```

As we saw above (Example 2.1), factor variables in data frames (case form or frequency form) can be re-ordered and declared as ordered factors using `ordered()`. As well, the order of the factors themselves can be rearranged by sorting the data frame using `sort()`.

However, in table form, the values of the table factors are ordered by their position in the table. Thus in the `JobSat` data, both `income` and `satisfaction` represent ordered factors, and the *positions* of the values in the rows and columns reflects their ordered nature, but only implicitly.

Yet, for analysis or graphing, there are occasions when you need *numeric* values for the levels of ordered factors in a table, e.g., to treat a factor as a quantitative variable. In such cases, you can

⁴There are quite a few functions in R with specialized methods for "table" objects. For example, `plot(GSS.tab)` gives a mosaic plot and `barchart(GSS.tab)` gives a divided bar chart.

simply re-assign the `dimnames` attribute of the table variables. For example, here, we assign numeric values to `income` as the middle of their ranges, and treat `satisfaction` as equally spaced with integer scores.

```
dimnames(JobSat)$income <- c(7.5, 20, 32.5, 60)
dimnames(JobSat)$satisfaction <- 1:4
```

A related case is when you want to preserve the character labels of table dimensions, but also allow them to be sorted in some particular order. A simple way to do this is to prefix each label with an integer index using `paste()`.

```
dimnames(JobSat)$income <- paste(1:4, dimnames(JobSat)$income, sep=":")
dimnames(JobSat)$satisfaction <-
  paste(1:4, dimnames(JobSat)$satisfaction, sep=": ")
```

A different situation arises with tables where you want to *permute* the levels of one or more variables to arrange them in a more convenient order without changing their labels. For example, in the `HairEyeColor` table, hair color and eye color are ordered arbitrarily. For visualizing the data using mosaic plots and other methods described later, it turns out to be more useful to assure that both hair color and eye color are ordered from dark to light. Hair colors are actually ordered this way already: "Black", "Brown", "Red", "Blond". But eye colors are ordered as "Brown", "Blue", "Hazel", "Green". It is easiest to re-order the eye colors by indexing the columns (dimension 2) in this array to a new order, "Brown", "Hazel", "Green", "Blue", giving the indices of the old levels in the new order (here: 1,3,4,2). Again `str()` is your friend, showing the structure of the result to check that the result is what you want.

```
data(HairEyeColor, package="datasets")
HEC <- HairEyeColor[, c(1,3,4,2), ]
str(HEC)

##  num [1:4, 1:4, 1:2] 32 53 10 3 10 25 7 5 3 15 ...
##  - attr(*, "dimnames")=List of 3
##    ..$ Hair: chr [1:4] "Black" "Brown" "Red" "Blond"
##    ..$ Eye : chr [1:4] "Brown" "Hazel" "Green" "Blue"
##    ..$ Sex : chr [1:2] "Male" "Female"
```

Finally, there are situations where, particularly for display purposes, you want to re-order the *dimensions* of an n -way table, and/or change the labels for the variables or levels. This is easy when the data are in table form: `aperm()` permutes the dimensions, and assigning to `names` and `dimnames` changes variable names and level labels respectively.

```
str(UCBAdmissions)

##  table [1:2, 1:2, 1:6] 512 313 89 19 353 207 17 8 120 205 ...
##  - attr(*, "dimnames")=List of 3
##    ..$ Admit : chr [1:2] "Admitted" "Rejected"
##    ..$ Gender: chr [1:2] "Male" "Female"
##    ..$ Dept  : chr [1:6] "A" "B" "C" "D" ...

UCB <- aperm(UCBAdmissions, c(2, 1, 3))
dimnames(UCB)[[2]] <- c("Yes", "No")
names(dimnames(UCB)) <- c("Sex", "Admitted", "Department")
str(UCB)
```

```
## table [1:2, 1:2, 1:6] 512 89 313 19 353 17 207 8 120 202 ...
## - attr(*, "dimnames")=List of 3
## ..$ Sex : chr [1:2] "Male" "Female"
## ..$ Admitted : chr [1:2] "Yes" "No"
## ..$ Department: chr [1:6] "A" "B" "C" "D" ...
```

2.4 Generating tables with `table()` and `xtabs()`

{sec:table}

With data in case form or frequency form, you can generate frequency tables from factor variables in data frames using the `table()` function; for tables of proportions, use the `prop.table()` function, and for marginal frequencies (summing over some variables) use `margin.table()`. The examples below use the same case-form data frame `mydata` used earlier (Section 2.1.4).

```
set.seed(12345) # reproducibility
n=100
A <- factor(sample(c("a1", "a2"), n, rep=TRUE))
B <- factor(sample(c("b1", "b2"), n, rep=TRUE))
sex <- factor(sample(c("M", "F"), n, rep=TRUE))
age <- round(rnorm(n, mean=30, sd=5))
mydata <- data.frame(A, B, sex, age)
```

`table(...)` takes a list of variables interpreted as factors, or a data frame whose columns are so interpreted. It does not take a `data=` argument, so either supply the names of columns in the data frame, or select the variables using column indexes:

```
# 2-Way Frequency Table
table(mydata$A, mydata$B) # A will be rows, B will be columns

##
##      b1 b2
## a1 18 30
## a2 22 30

(mytab <- table(mydata[,1:2])) # same

##      B
## A    b1 b2
## a1 18 30
## a2 22 30
```

We can use `margin.table(X, margin)` to sum a table `X` for the indices in `margin`, i.e., over the dimensions not included in `margin`. A related function is `addmargins(X, margin, FUN=sum)`, which extends the dimensions of a table or array with the marginal values calculated by `FUN`.

```
margin.table(mytab) # sum over A & B

## [1] 100

margin.table(mytab, 1) # A frequencies (summed over B)

## A
## a1 a2
## 48 52
```

```
margin.table(mytab, 2) # B frequencies (summed over A)

## B
## b1 b2
## 40 60

addmargins(mytab) # show all marginal totals

##      B
## A    b1  b2 Sum
## a1  18  30  48
## a2  22  30  52
## Sum 40  60 100
```

The function `prop.table()` expresses the table entries as a fraction of a given marginal table.

```
prop.table(mytab) # cell percentages

##      B
## A    b1  b2
## a1 0.18 0.30
## a2 0.22 0.30

prop.table(mytab, 1) # row percentages

##      B
## A    b1  b2
## a1 0.37500 0.62500
## a2 0.42308 0.57692

prop.table(mytab, 2) # column percentages

##      B
## A    b1  b2
## a1 0.45 0.50
## a2 0.55 0.50
```

`table()` can also generate multidimensional tables based on 3 or more categorical variables. In this case, use the `ftable()` or `structable()` function to print the results more attractively as a “flat” (2-way) table.

```
# 3-Way Frequency Table
mytab <- table(mydata[,c("A", "B", "sex")])
ftable(mytab)

##      sex  F  M
## A  B
## a1 b1      9  9
##    b2     15 15
## a2 b1     12 10
##    b2     19 11
```

`table()` ignores missing values by default, but has optional arguments `useNA` and `exclude` that can be used to control this. See `help(table)` for the details.

2.4.1 xtabs()

{sec:xtabs}

The `xtabs()` function allows you to create cross tabulations of data using formula style input. This typically works with case-form or frequency-form data supplied in a data frame or a matrix. The result is a contingency table in array format, whose dimensions are determined by the terms on the right side of the formula. As shown below, the `summary` method for tables produces a simple χ^2 test of independence of all factors.

```
# 3-Way Frequency Table
mytable <- xtabs(~A+B+sex, data=mydata)
ftable(mytable) # print table

##           sex  F  M
## A  B
## a1 b1         9  9
##     b2        15 15
## a2 b1        12 10
##     b2        19 11

summary(mytable) # chi-square test of independence

## Call: xtabs(formula = ~A + B + sex, data = mydata)
## Number of cases in table: 100
## Number of factors: 3
## Test for independence of all factors:
##  Chisq = 1.54, df = 4, p-value = 0.82
```

When the data have already been tabulated in frequency form, include the frequency variable (usually `count` or `Freq`) on the left side of the formula, as shown in the example below for the GSS data.

```
(GSStab <- xtabs(count ~ sex + party, data=GSS))

##           party
## sex      dem indep rep
## female 279     73 225
## male   165     47 191

summary(GSStab)

## Call: xtabs(formula = count ~ sex + party, data = GSS)
## Number of cases in table: 980
## Number of factors: 2
## Test for independence of all factors:
##  Chisq = 7, df = 2, p-value = 0.03
```

For "table" objects, the `plot` method produces basic mosaic plots using the `mosaicplot()` function. With the option `shade=TRUE`, the cells are shaded according to the deviations (residuals) from an independence model. Mosaic plots are discussed in detail in Chapter 5.

```
plot(mytable)
plot(GSStab, shade=TRUE)
```

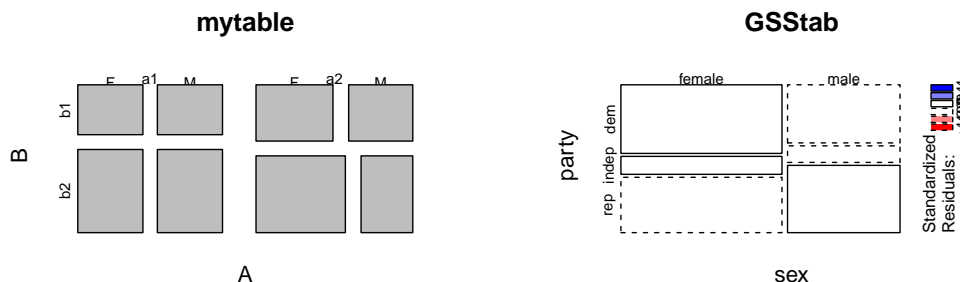



Figure 2.2: Mosaic plot of tables using the plot method for table objects fig:plot-xtab

2.5 Printing tables with `structable()` and `ftable()`

`structable()`

For 3-way and larger tables, the functions `ftable()` (in the `stats` package) and `structable()` (in `vcd`) provide a convenient and flexible tabular display in a “flat” (2-way) format.

With `ftable(X, row.vars=, col.vars=)`, variables assigned to the rows and/or columns of the result can be specified as the integer numbers or character names of the variables in the array `X`. By default, the last variable is used for the columns. The formula method, in the form `ftable(colvars ~ rowvars, data)` allows a formula, where the left and right hand side of formula specify the column and row variables respectively.

```
ftable(UCB) # default
##           Department  A  B  C  D  E  F
## Sex      Admitted
## Male    Yes         512 353 120 138 53 22
##         No         313 207 205 279 138 351
## Female  Yes          89 17 202 131 94 24
##         No          19  8 391 244 299 317

#ftable(UCB, row.vars=1:2) # same result
ftable(Admitted + Sex ~ Department, data=UCB) # formula method
##           Admitted  Yes           No
##           Sex      Male Female Male Female
## Department
## A           512     89    313     19
## B           353     17    207     8
## C           120    202    205    391
## D           138    131    279    244
## E            53     94    138    299
## F            22     24    351    317
```

The `structable()` function is similar, but more general, and uses recursive splits in the vertical or horizontal directions (similar to the construction of mosaic displays). It works with both data frames and table objects.

```
structable(HairEyeColor) # show the table: default
##           Eye Brown Blue Hazel Green
```

```
## Hair Sex
## Black Male 32 11 10 3
## Female 36 9 5 2
## Brown Male 53 50 25 15
## Female 66 34 29 14
## Red Male 10 10 7 7
## Female 16 7 7 7
## Blond Male 3 30 5 8
## Female 4 64 5 8

structable(Hair+Sex ~ Eye, HairEyeColor) # specify col ~ row variables

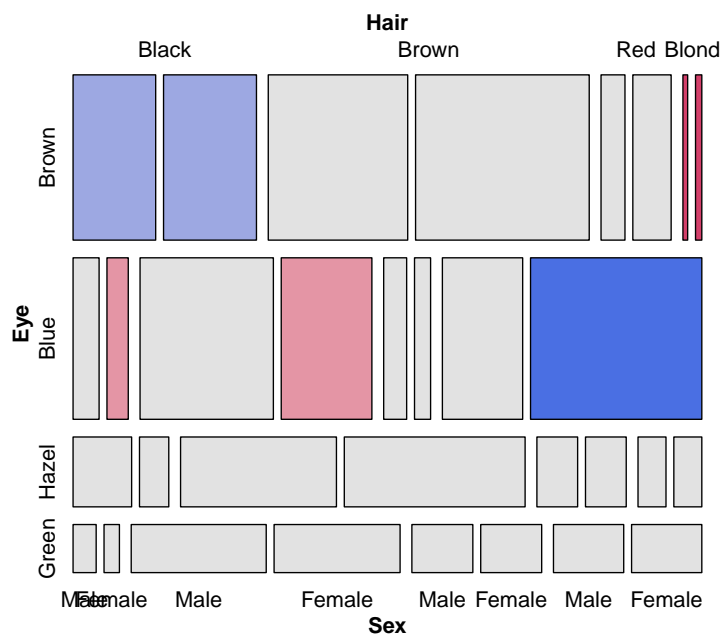
## Hair Black Brown Red Blond
## Sex Male Female Male Female Male Female Male Female Male Female
## Eye
## Brown 32 36 53 66 10 16 3 4
## Blue 11 9 50 34 10 7 30 64
## Hazel 10 5 25 29 7 7 5 5
## Green 3 2 15 14 7 7 8 8
```

It also returns an object of class "structable" for which there are a variety of special methods. For example, the transpose function `t()` interchanges rows and columns, so that `t(structable(HairEyeColor))` produces the second result shown just above; "structable" objects can be subset using the `[]` and `[[` operators, using either level indices or names. There are also plot methods, so that `plot()` and `mosaic()` produce mosaic plots.

```
HSE <- structable(Hair+Sex ~ Eye, HairEyeColor) # save structable object
HSE[1:2,] # subset rows

## Hair Black Brown Red Blond
## Sex Male Female Male Female Male Female Male Female Male Female
## Eye
## Brown 32 36 53 66 10 16 3 4
## Blue 11 9 50 34 10 7 30 64

mosaic(HSE, shade=TRUE, legend=FALSE) # plot it
```



2.5.1 Publishing tables to L^AT_EX or HTML

OK, you’ve read your data into R, done some analysis, and now want to include some tables in a L^AT_EX document or in a web page in HTML format. Formatting tables for these purposes is often tedious and error-prone.

There are a great many packages in R that provide for nicely formatted, publishable tables for a wide variety of purposes; indeed, most of the tables in this book are generated using these tools. See Leifeld (2013) for description of the `texreg` package and a comparison with some of the other packages.

Here, we simply illustrate the `xtable` package, which, along with capabilities for statistical model summaries, time-series data, and so forth, has a `xtable.table` method for one-way and two-way table objects.

The `HorseKicks` data is a small one-way frequency table described in Example 3.4 and containing the frequencies of 0, 1, 2, 3, 4 deaths per corps-year by horse-kick among soldiers in 20 corps in the Prussian army.

```
data(HorseKicks, package="vcd")
HorseKicks

## nDeaths
##    0    1    2    3    4
## 109   65   22    3    1
```

By default, `xtable()` formats this in L^AT_EX as a vertical table, and prints the L^AT_EX markup to the R console. This output is shown below (without the usual `##` comment used to indicate R output).

```
library(xtable)
xtable(HorseKicks)

% latex table generated in R 3.1.1 by xtable 1.7-4 package
% Mon Nov 17 14:53:27 2014
\begin{table}[ht]
\centering
\begin{tabular}{rr}
\hline
& nDeaths \\
\hline
0 & 109 \\
1 & 65 \\
2 & 22 \\
3 & 3 \\
4 & 1 \\
\hline
\end{tabular}
\end{table}
```

When this is rendered in a L^AT_EX document, the result of `xtable()` appears as shown in the table below.

```
xtable(HorseKicks)
```

The table above isn’t quite right, because the column label “nDeaths” belongs to the first column, and the second column should be labeled “Freq”. To correct that, we convert the

nDeaths	
0	109
1	65
2	22
3	3
4	1

HorseKicks table to a data frame (see Section 2.7 for details), add the appropriate colnames, and use the `xtable.print` method to supply some other options.

```
tab <- as.data.frame(HorseKicks)
colnames(tab) <- c("nDeaths", "Freq")
print(xtable(tab), include.rownames=FALSE, include.colnames=TRUE)
```

nDeaths	Freq
0	109
1	65
2	22
3	3
4	1

Finally, in Chapter 3, we display a number of similar one-way frequency tables in a transposed form to save display space. Table 3.3 is the finished version we show there. The code below uses the following techniques: (a) `addmargins()` is used to show the sum of all the frequency values; (b) `t()` transposes the data frame to have 2 rows; (c) `rownames()` assigns the labels we want for the rows; (d) using the `caption` argument provides a table caption, and a numbered table in L^AT_EX. (e) column alignment ("`r`" or "`l`") for the table columns is computed as a character string used for the `align` argument.

```
horsetab <- t( as.data.frame( addmargins( HorseKicks ) ) )
rownames( horsetab ) <- c( "Number of deaths", "Frequency" )
horsetab <- xtable( horsetab, digits = 0,
  caption = "von Bortkiewicz's data on deaths by horse kicks",
  align = paste0("l|", paste(rep("r", ncol(horsetab)), collapse=""))
)
print(horsetab, include.colnames=FALSE)
```

Number of deaths	0	1	2	3	4	Sum
Frequency	109	65	22	3	1	200

Table 2.1: von Bortkiewicz's data on deaths by horse kicks

2.6 Collapsing over table factors: `aggregate()`, `margin.table()` and `apply()`

`c:collapse}`

It sometimes happens that we have a data set with more variables or factors than we want to analyse, or else, having done some initial analyses, we decide that certain factors are not important, and so should be excluded from graphic displays by collapsing (summing) over them. For example, mosaic plots and fourfold displays are often simpler to construct from versions of the data collapsed over the factors which are not shown in the plots.

The appropriate tools to use again depend on the form in which the data are represented—a case-form data frame, a frequency-form data frame (`aggregate()`), or a table-form array or table object (`margin.table()` or `apply()`).

When the data are in frequency form, and we want to produce another frequency data frame, `aggregate()` is a handy tool, using the argument `FUN=sum` to sum the frequency variable over the factors *not* mentioned in the formula.

`{ex:dayton1}`

EXAMPLE 2.6: Dayton survey

The data frame `DaytonSurvey` in the `vcdExtra` package represents a 2^5 table giving the frequencies of reported use (“ever used?”) of alcohol, cigarettes and marijuana in a sample of 2276 high school seniors, also classified by sex and race.

```
data(DaytonSurvey, package="vcdExtra")
str(DaytonSurvey)

## 'data.frame': 32 obs. of 6 variables:
## $ cigarette: Factor w/ 2 levels "Yes", "No": 1 2 1 2 1 2 1 2 1 2 ...
## $ alcohol  : Factor w/ 2 levels "Yes", "No": 1 1 2 2 1 1 2 2 1 1 ...
## $ marijuana: Factor w/ 2 levels "Yes", "No": 1 1 1 1 2 2 2 2 1 1 ...
## $ sex      : Factor w/ 2 levels "female", "male": 1 1 1 1 1 1 1 1 2 2 ...
## $ race     : Factor w/ 2 levels "white", "other": 1 1 1 1 1 1 1 1 1 1 ...
## $ Freq     : num 405 13 1 1 268 218 17 117 453 28 ...

head(DaytonSurvey)

##   cigarette alcohol marijuana   sex   race Freq
## 1      Yes      Yes      Yes female white 405
## 2      No      Yes      Yes female white  13
## 3      Yes      No      Yes female white   1
## 4      No      No      Yes female white   1
## 5      Yes      Yes      No  female white 268
## 6      No      Yes      No  female white 218
```

To focus on the associations among the substances, we want to collapse over sex and race. The right-hand side of the formula used in the call to `aggregate()` gives the factors to be retained in the new frequency data frame, `Dayton.ACM.df`. The left-hand side is the frequency variable (`Freq`), and we aggregate using the `FUN=sum`.

```
# data in frequency form: collapse over sex and race
Dayton.ACM.df <- aggregate(Freq ~ cigarette+alcohol+marijuana,
                           data=DaytonSurvey, FUN=sum)
Dayton.ACM.df

##   cigarette alcohol marijuana Freq
```

```
## 1      Yes      Yes      Yes  911
## 2      No       Yes      Yes   44
## 3      Yes      No       Yes    3
## 4      No       No       Yes    2
## 5      Yes      Yes      No  538
## 6      No       Yes      No  456
## 7      Yes      No       No   43
## 8      No       No       No  279
```

△

When the data are in table form, and we want to produce another table, `apply()` with `FUN=sum` can be used in a similar way to sum the table over dimensions not mentioned in the `MARGIN` argument. `margin.table()` is just a wrapper for `apply()` using the `sum()` function.

```
{ex:dayton2}
```

EXAMPLE 2.7: Dayton survey

To illustrate, we first convert the `DaytonSurvey` to a 5-way table using `xtabs()`, giving `Dayton.tab`.

```
# convert to table form
Dayton.tab <- xtabs(Freq~cigarette+alcohol+marijuana+sex+race,
                   data=DaytonSurvey)
structable(cigarette+alcohol+marijuana ~ sex+race, data=Dayton.tab)

##           cigarette Yes      No      No
##           alcohol  Yes      No      Yes      No
##           marijuana Yes  No Yes  No Yes  No Yes  No
## sex    race
## female white      405 268   1  17  13 218   1 117
##         other      23  23   0   1   2  19   0  12
## male   white      453 228   1  17  28 201   1 133
##         other      30  19   1   8   1  18   0  17
```

Then, use `apply()` on `Dayton.tab` to give the 3-way table `Dayton.ACM.tab` summed over sex and race. The elements in this new table are the column sums for `Dayton.tab` shown by `structable()` just above.

```
# collapse over sex and race
Dayton.ACM.tab <- apply(Dayton.tab, MARGIN=1:3, FUN=sum)
Dayton.ACM.tab <- margin.table(Dayton.tab, 1:3) # same result
structable(cigarette+alcohol ~ marijuana, data=Dayton.ACM.tab)

##           cigarette Yes      No
##           alcohol  Yes  No Yes  No
## marijuana
## Yes           911   3  44   2
## No           538  43 456 279
```

△

Many of these operations can be performed using the `**ply()` functions in the `plyr` package. For example, with the data in a frequency form data frame, use `ddply()` to collapse over unmentioned factors, and `plyr::summarise()`⁵ as the function to be applied to each piece.

⁵Ugh. This `plyr` function clashes with a function of the same name in `vcdExtra`. In this book I will use the explicit double-colon notation to keep them separate.

```
Dayton.ACM.df <- ddpily(DaytonSurvey, .(cigarette, alcohol, marijuana),
  plyr::summarise, Freq=sum(Freq))
```

2.6.1 Collapsing table levels: collapse.table()

A related problem arises when we have a table or array and for some purpose we want to reduce the number of levels of some factors by summing subsets of the frequencies. For example, we may have initially coded Age in 10-year intervals, and decide that, either for analysis or display purposes, we want to reduce Age to 20-year intervals. The `collapse.table()` function in `vcdExtra` was designed for this purpose.

{ex:collapse-cat}

EXAMPLE 2.8: Collapsing categories

Create a 3-way table, and collapse Age from 10-year to 20-year intervals and Education from three levels to two. To illustrate, we first generate a $2 \times 6 \times 3$ table of random counts from a Poisson distribution with mean of 100, with factors *sex*, *age* and *education*.

```
# create some sample data in frequency form
sex <- c("Male", "Female")
age <- c("10-19", "20-29", "30-39", "40-49", "50-59", "60-69")
education <- c("low", "med", "high")
dat <- expand.grid(sex=sex, age=age, education=education)
counts <- rpois(36, 100) # random Poisson cell frequencies
dat <- cbind(dat, counts)
# make it into a 3-way table
tab1 <- xtabs(counts ~ sex + age + education, data=dat)
structable(tab1)
```

##	##	##	age	10-19	20-29	30-39	40-49	50-59	60-69
##	sex	education							
##	Male	low		91	110	106	95	107	98
##		med		108	104	97	100	107	112
##		high		104	104	106	101	92	95
##	Female	low		115	103	96	93	112	94
##		med		96	88	92	103	98	93
##		high		84	93	103	93	95	103

Now collapse age to 20-year intervals, and education to 2 levels. In the arguments to `collapse.table()`, levels of age and education given the same label are summed in the resulting smaller table.

```
# collapse age to 3 levels, education to 2 levels
tab2 <- collapse.table(tab1,
  age=c("10-29", "10-29", "30-49", "30-49", "50-69", "50-69"),
  education=c("<high", "<high", "high"))
structable(tab2)
```

##	##	##	age	10-29	30-49	50-69
##	sex	education				
##	Male	<high		413	398	424
##		high		208	207	187
##	Female	<high		402	384	397
##		high		177	196	198

△

2.7 Converting among frequency tables and data frames

{sec:conver

As we've seen, a given contingency table can be represented equivalently in case form, frequency form and table form. However, some R functions were designed for one particular representation. Table 2.2 shows some handy tools for converting from one form to another.

{tab:convert}

Table 2.2: Tools for converting among different forms for categorical data

From this	To this		
	Case form	Frequency form	Table form
Case form		<code>Z <- xtabs(A+B)</code> <code>as.data.frame(Z)</code>	<code>table(A,B)</code>
Frequency form	<code>expand.dft(X)</code>		<code>xtabs(count~A+B)</code>
Table form	<code>expand.dft(X)</code>	<code>as.data.frame(X)</code>	

2.7.1 Table form to frequency form

A contingency table in table form (an object of class "table") can be converted to a data frame in frequency form with `as.data.frame()`.⁶ The resulting data frame contains columns representing the classifying factors and the table entries (as a column named by the `responseName` argument, defaulting to `Freq`). The function `as.data.frame()` is the inverse of `xtabs()`, which converts a data frame to a table.

{ex:GSS-convert}

EXAMPLE 2.9: General social survey

Convert the `GSStab` in table form to a data.frame in frequency form. By default, the frequency variable is named `Freq`, and the variables `sex` and `party` are made factors.

```
as.data.frame(GSStab)

##      sex party Freq
## 1 female  dem  279
## 2 male    dem  165
## 3 female indep   73
## 4 male    indep  47
## 5 female  rep  225
## 6 male    rep  191
```

△

In addition, there are situations where numeric table variables are represented as factors, but you need to convert them to numerics for calculation purposes.

{ex:horse.df}

EXAMPLE 2.10: Death by horse kick

For example, We might want to calculate the weighted mean of `nDeaths` in the `HorseKicks` data. Using `as.data.frame()` won't work here, because the variable `nDeaths` becomes a factor.

⁶Because R is object-oriented, this is actually a short-hand for the function `as.data.frame.table()`.


```
str(as.data.frame(HorseKicks))

## 'data.frame': 5 obs. of 2 variables:
## $ nDeaths: Factor w/ 5 levels "0","1","2","3",...: 1 2 3 4 5
## $ Freq   : int  109 65 22 3 1
```

One solution is to use `data.frame()` directly and `as.numeric()` to coerce the table names to numbers.

```
horse.df <- data.frame(nDeaths = as.numeric(names(HorseKicks)),
                      Freq = as.vector(HorseKicks))
str(horse.df)

## 'data.frame': 5 obs. of 2 variables:
## $ nDeaths: num  0 1 2 3 4
## $ Freq   : int  109 65 22 3 1

horse.df

##   nDeaths Freq
## 1      0  109
## 2      1   65
## 3      2   22
## 4      3    3
## 5      4    1
```

Then, `weighted.mean()` works as we would like:

```
weighted.mean(horse.df$nDeaths, weights=horse.df$Freq)

## [1] 2
```

△

2.7.2 Case form to table form

Going the other way, we use `table()` to convert from case form to table form.

{ex:Arth-convert}

EXAMPLE 2.11: Arthritis treatment

Convert the Arthritis data in case form to a 3-way table of Treatment \times Sex \times Improved. We select the desired columns with their names, but could also use column numbers, e.g., `table(Arthritis[,c(2, 3, 5)])`.

```
Art.tab <- table(Arthritis[,c("Treatment", "Sex", "Improved")])
str(Art.tab)

## 'table' int [1:2, 1:2, 1:3] 19 6 10 7 7 5 0 2 6 16 ...
## - attr(*, "dimnames")=List of 3
## ..$ Treatment: chr [1:2] "Placebo" "Treated"
## ..$ Sex       : chr [1:2] "Female" "Male"
## ..$ Improved : chr [1:3] "None" "Some" "Marked"

ftable(Art.tab)
```

```
##           Improved None Some Marked
## Treatment Sex
## Placebo  Female      19    7     6
##           Male       10    0     1
## Treated  Female      6    5    16
##           Male       7    2     5
```

△

2.7.3 Table form to case form

There may also be times that you will need an equivalent case form data frame with factors representing the table variables rather than the frequency table. For example, the `mca()` function in package `MASS` only operates on data in this format. The function `expand.dft()`⁷ in `vcdExtra` does this, converting a table into a case form.

{ex:Arth-convert2}

EXAMPLE 2.12: Arthritis treatment

Convert the `Arthritis` data in table form (`Art.tab`) back to a `data.frame` in case form, with factors `Treatment`, `Sex` and `Improved`.

```
Art.df <- expand.dft(Art.tab)
str(Art.df)

## 'data.frame': 84 obs. of 3 variables:
## $ Treatment: Factor w/ 2 levels "Placebo","Treated": 1 1 1 1 1 1 1 1 1 1 ...
## $ Sex      : Factor w/ 2 levels "Female","Male": 1 1 1 1 1 1 1 1 1 1 ...
## $ Improved : Factor w/ 3 levels "Marked","None",...: 2 2 2 2 2 2 2 2 2 2 ...
```

△

2.8 A complex example: TV viewing data

If you've followed so far, congratulations! You're ready for a more complicated example that puts together a variety of the skills developed in this chapter: (a) reading raw data, (b) creating tables, (c) assigning level names to factors and (d) collapsing levels or variables for use in analysis.

For illustration of these steps, we use the dataset `tv.dat`, supplied with the initial implementation of mosaic displays in `R` by Jay Emerson. In turn, they were derived from an early, compelling example of mosaic displays (Hartigan and Kleiner, 1984), that illustrated the method with data on a large sample of TV viewers whose behavior had been recorded for the Nielsen ratings. This data set contains sample television audience data from Nielsen Media Research for the week starting November 6, 1995.

The data file, `tv.dat` is stored in frequency form as a file with 825 rows and 5 columns. There is no header line in the file, so when we use `read.table()` below, the variables will be named `V1 - V5`. This data represents a 4-way table of size $5 \times 11 \times 5 \times 3 = 825$ where the table variables are `V1 - V4`, and the cell frequency is read as `V5`.

The table variables are:

`V1- values 1:5` correspond to the days Monday–Friday;

⁷The original code for this function was provided by Marc Schwarz on the R-Help mailing list.

sec:working-complex}

V2– values 1:11 correspond to the quarter hour times 8:00PM through 10:30PM;
 V3– values 1:5 correspond to ABC, CBS, NBC, Fox, and non-network choices;
 V4– values 1:3 correspond to transition states: turn the television Off, Switch channels, or Persist in viewing the current channel.

2.8.1 Creating data frames and arrays

The file `tv.dat` is stored in the `doc/extdata` directory of `vcdExtra`; it can be read as follows:

```
tv.data<-read.table(system.file("doc","extdata","tv.dat",package="vcdExtra"))
str(tv.data)

## 'data.frame': 825 obs. of 5 variables:
## $ V1: int 1 2 3 4 5 1 2 3 4 5 ...
## $ V2: int 1 1 1 1 1 2 2 2 2 2 ...
## $ V3: int 1 1 1 1 1 1 1 1 1 1 ...
## $ V4: int 1 1 1 1 1 1 1 1 1 1 ...
## $ V5: int 6 18 6 2 11 6 29 25 17 29 ...

head(tv.data, 5)

##   V1 V2 V3 V4 V5
## 1  1  1  1  1  6
## 2  2  1  1  1 18
## 3  3  1  1  1  6
## 4  4  1  1  1  2
## 5  5  1  1  1 11
```

To read such data from a local file, just use `read.table()` in this form:

```
tv.data<-read.table("C:/R/data/tv.dat")
```

We could use this data in frequency form for analysis by renaming the variables, and converting the integer-coded factors V1 – V4 to R factors. The lines below use the function `within()` to avoid having to use `TV.dat$Day <- factor(TV.dat$Day)` etc., and only supplies labels for the first variable.

```
TV.df <- tv.data
colnames(TV.df) <- c("Day", "Time", "Network", "State", "Freq")
TV.df <- within(TV.df, {Day <- factor(Day,
                                   labels=c("Mon", "Tue", "Wed", "Thu", "Fri"))
                Time <- factor(Time)
                Network <- factor(Network)
                State <- factor(State)})
```

Alternatively, we could just reshape the frequency column (V5 or `tv.data[, 5]`) into a 4-way array. In the lines below, we rely on the facts that the (a) the table is complete— there are no missing cells, so `nrow(tv.data)=825`; (b) the observations are ordered so that V1 varies most rapidly and V4 most slowly. From this, we can just extract the frequency column and reshape it into an array using the `dim` argument. The level names are assigned to `dimnames(TV)` and the variable names to `names(dimnames(TV))`.

```
TV <- array(tv.data[,5], dim=c(5,11,5,3))
dimnames(TV) <- list(c("Mon", "Tue", "Wed", "Thu", "Fri"),
                   c("8:00", "8:15", "8:30", "8:45", "9:00", "9:15", "9:30",
```

```

      "9:45", "10:00", "10:15", "10:30"),
    c("ABC", "CBS", "NBC", "Fox", "Other"),
    c("Off", "Switch", "Persist"))
names(dimnames(TV)) <- c("Day", "Time", "Network", "State")

```

More generally (even if there are missing cells), we can use `xtabs()` (or `plyr::dply()`) to do the cross-tabulation, using `V5` as the frequency variable. Here's how to do this same operation with `xtabs()`:

```

TV <- xtabs(V5 ~ ., data=tv.data)
dimnames(TV) <- list(Day=c("Mon", "Tue", "Wed", "Thu", "Fri"),
                    Time=c("8:00", "8:15", "8:30", "8:45", "9:00", "9:15", "9:30",
                          "9:45", "10:00", "10:15", "10:30"),
                    Network=c("ABC", "CBS", "NBC", "Fox", "Other"),
                    State=c("Off", "Switch", "Persist"))

```

Note that in the lines above, the variable names are assigned directly as the names of the elements in the `dimnames` list.

2.8.2 Subsetting and collapsing

For many purposes, the 4-way table `TV` is too large and awkward to work with. Among the networks, `Fox` and `Other` occur infrequently, so we will remove them. We can also cut it down to a 3-way table by considering only viewers who persist with the current station.⁸

```

TV <- TV[, , 1:3, ] # keep only ABC, CBS, NBC
TV <- TV[, , 3] # keep only Persist -- now a 3 way table
structable(TV)

##           Time 8:00 8:15 8:30 8:45 9:00 9:15 9:30 9:45 10:00 10:15 10:30
## Day Network
## Mon ABC      146  151  156   83  325  350  386  340  352  280  278
##      CBS      337  293  304  233  311  251  241  164  252  265  272
##      NBC      263  219  236  140  226  235  239  246  279  263  283
## Tue ABC      244  181  231  205  385  283  345  192  329  351  364
##      CBS      173  180  184  109  218  235  256  250  274  263  261
##      NBC      315  254  280  241  370  214  195  111  188  190  210
## Wed ABC      233  161  194  156  339  264  279  140  237  228  203
##      CBS      158  126  207   59   98  103  122   86  109  105  110
##      NBC      134  146  166   66  194  230  264  143  274  289  306
## Thu ABC      174  183  197  181  187  198  211   86  110  122  117
##      CBS      196  185  195  104  106  116  116   47  102   84   84
##      NBC      515  463  472  477  590  473  446  349  649  705  747
## Fri ABC      294  281  305  239  278  246  245  138  246  232  233
##      CBS      130  144  154   81  129  153  136  126  138  136  152
##      NBC      195  220  248  160  172  164  169   85  183  198  204

```

Finally, for some purposes, we might also want to collapse the 11 times into a smaller number. Here, we use `as.data.frame.table()` to convert the table back to a data frame, `levels()` to re-assign the values of `Time`, and finally, `xtabs()` to give a new, collapsed frequency table.

⁸This relies on the fact that indexing an array drops dimensions of length 1 by default, using the argument `drop=TRUE`; the result is coerced to the lowest possible dimension.

```
TV.df <- as.data.frame.table(TV)
levels(TV.df$Time) <- c(rep("8:00-8:59", 4),
                       rep("9:00-9:59", 4), rep("10:00-10:44", 3))
TV2 <- xtabs(Freq ~ Day + Time + Network, TV.df)
structable(Day ~ Time+Network, TV2)
```

```
##           Day  Mon  Tue  Wed  Thu  Fri
## Time      Network
## 8:00-8:59  ABC      536  861  744  735 1119
##           CBS      1167  646  550  680  509
##           NBC      858 1090  512 1927  823
## 9:00-9:59  ABC      1401 1205 1022  682  907
##           CBS      967  959  409  385  544
##           NBC      946  890  831 1858  590
## 10:00-10:44 ABC      910 1044  668  349  711
##           CBS      789  798  324  270  426
##           NBC      825  588  869 2101  585
```

Congratulations! If you followed the operations described above, you are ready for the material described in the rest of the book. If not, try working through some of exercises below.

As a final step and a prelude to what follows, we construct a mosaic plot, below (Figure 2.3) that focuses on the associations between the combinations of Day and Time and the Network viewed. In terms of a loglinear model, this is represented by the model formula $\sim \text{Day}:\text{Time} + \text{Network}$, which asserts that Network is independent of the Day:Time combinations.

```
dimnames(TV2)$Time <- c("8", "9", "10") # re-level for mosaic display
mosaic(~ Day + Network + Time, data=TV2, expected=~Day:Time + Network,
       legend=FALSE, gp=shading_Friendly)
```

The cells shaded in blue show positive associations (observed frequency $>$ expected) and red shows negative associations. From this it is easy to read how network choice varies with day and time. For example, CBS dominates in all time slots on Monday; ABC and NBC dominate on Tuesday, particularly in the later time slots; Thursday is an NBC day, while on Friday, ABC gets the greatest share.

2.9 Further reading

{sec:ch02-reading}

If you're new to the R language but keen to get started with linear modeling or logistic regression in the language, take a look at this *Introduction to R*, <http://data.princeton.edu/R/introducingR.pdf>, by Germán Rodríguez.

2.10 Lab exercises

{lab:ch02-exercises}

Exercise 2.1 The packages `vcd` and `vcdExtra` contain many data sets with some examples of analysis and graphical display. The goal of this exercise is to familiarize yourself with these resources.

You can get a brief summary of these using the function `datasets()`. Use the following to get a list of these with some characteristics and titles.

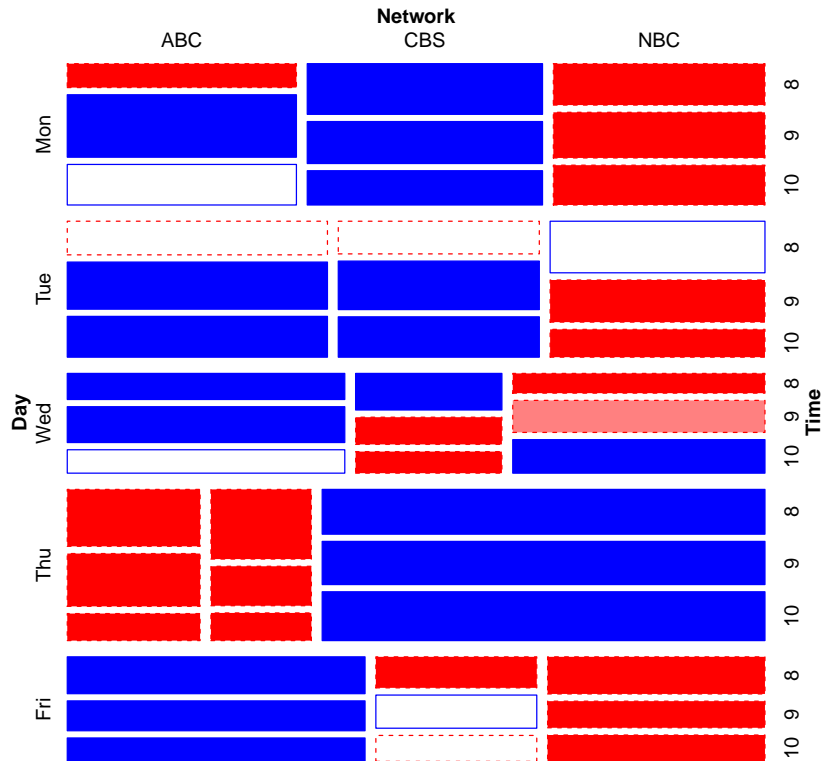


Figure 2.3: Mosaic plot for the TV data showing model of joint independence, Day:Time + Network

```
ds <- datasets(package=c("vcd", "vcdExtra"))
str(ds)

## 'data.frame': 70 obs. of 5 variables:
## $ Package: chr "vcd" "vcd" "vcd" "vcd" ...
## $ Item : chr "Arthritis" "Baseball" "BrokenMarriage" "Bundesliga" ...
## $ class : chr "data.frame" "data.frame" "data.frame" "data.frame" ...
## $ dim : chr "84x5" "322x25" "20x4" "14018x7" ...
## $ Title : chr "Arthritis Treatment Data" "Baseball Data" "Broken Marriage Data" "Ergel
```

- How many data sets are there altogether? How many are there in each package?
- Make a tabular display of the frequencies by Package and class.
- Choose one or two data sets from this list, and examine their help files (e.g., `help(Arthritis)` or `?Arthritis`). You can use, e.g., `example(Arthritis)` to run the R code for a given example.

{lab:2.2}

Exercise 2.2 The data set `UCBADmissions` is a 3-way table of frequencies classified by `Admit`, `Gender` and `Dept`.

- Find the total number of cases contained in this table.
- For each department, find the total number of applicants.
- For each department, find the overall proportion of applicants who were admitted.

- (d) Construct a tabular display of department (rows) and gender (columns), showing the proportion of applicants in each cell who were admitted.

{lab:2.3}

Exercise 2.3 The data set `DanishWelfare` in `vcd` gives a 4-way, $3 \times 4 \times 3 \times 5$ table as a data frame in frequency form, containing the variable `Freq` and four factors, `Alcohol`, `Income`, `Status` and `Urban`. The variable `Alcohol` can be considered as the response variable, and the others as possible predictors.

- Find the total number of cases represented in this table.
- In this form, the variables `Alcohol` and `Income` should arguably be considered *ordered* factors. Change them to make them ordered.
- Convert this data frame to table form, `DanishWelfare.tab`, a 4-way array containing the frequencies with appropriate variable names and level names.
- The variable `Urban` has 5 categories. Find the total frequencies in each of these. How would you collapse the table to have only two categories, `City`, `Non-city`?
- Use `structable()` or `ftable()` to produce a pleasing flattened display of the frequencies in the 4-way table. Choose the variables used as row and column variables to make it easier to compare levels of `Alcohol` across the other factors.

{lab:2.4}

Exercise 2.4 The data set `UKSoccer` in `vcd` gives the distributions of number of goals scored by the 20 teams in the 1995/96 season of the Premier League of the UK Football Association.

```
data(UKSoccer, package="vcd")
ftable(UKSoccer)

##      Away  0  1  2  3  4
## Home
## 0      27 29 10  8  2
## 1      59 53 14 12  4
## 2      28 32 14 12  4
## 3      19 14  7  4  1
## 4       7  8 10  2  0
```

This two-way table classifies all $20 \times 19 = 380$ games by the joint outcome (Home, Away), the number of goals scored by the Home and Away teams. The value 4 in this table actually represents 4 or more goals.

- Verify that the total number of games represented in this table is 380.
- Find the marginal total of the number of goals scored by each of the home and away teams.
- Express each of the marginal totals as proportions.
- Comment on the distribution of the numbers of home-team and away-team goals. Is there any evidence that home teams score more goals on average?

{lab:2.5}

Exercise 2.5 The one-way frequency table, `Saxony` in `vcd` records the frequencies of families with 0, 1, 2, ... 12 male children, among 6115 families with 12 children. This data set is used extensively in Chapter 3.

```
data(Saxony, package="vcd")
Saxony

## nMales
## 0  1  2  3  4  5  6  7  8  9 10 11 12
## 3 24 104 286 670 1033 1343 1112 829 478 181 45 7
```

Another data set, `Geissler` in the `vcdExtra` package, gives the complete tabulation of all combinations of boys and girls in families with a given total number of children `size`. The task here is to create an equivalent table, `Saxony12` from the `Geissler` data.

```
data(Geissler, package="vcdExtra")
str(Geissler)

## 'data.frame': 90 obs. of 4 variables:
## $ boys : int 0 0 0 0 0 0 0 0 0 0 ...
## $ girls: num 1 2 3 4 5 6 7 8 9 10 ...
## $ size : num 1 2 3 4 5 6 7 8 9 10 ...
## $ Freq : int 108719 42860 17395 7004 2839 1096 436 161 66 30 ...
```

- Use `subset()` to create a data frame, `sax12` containing the `Geissler` observations in families with `size==12`.
- Select the columns for `boys` and `Freq`.
- Use `xtabs()` with a formula, `Freq ~ boys`, to create the one-way table.
- Do the same steps again, to create a one-way table, `Saxony11` containing similar frequencies for families of `size==11`.

{lab:2.6}

Exercise 2.6 *Interactive coding of table factors*: Some statistical and graphical \star methods for contingency tables are implemented only for two-way tables, but can be extended to 3+ way tables by recoding the factors to interactive combinations along the rows and/or columns, in a way similar to what `ftable()` and `structable()` do for printed displays.

For the `UCBAdmissions` data, produce a two-way table object, `UCB.tab2` that has the combinations of `Admit` and `Gender` as the rows, and `Dept` as its columns, to look like the result below:

	Dept					
Admit:Gender	A	B	C	D	E	F
Admitted:Female	89	17	202	131	94	24
Admitted:Male	512	353	120	138	53	22
Rejected:Female	19	8	391	244	299	317
Rejected:Male	313	207	205	279	138	351

{lab:2.7}

Hint: convert to a data frame, manipulate the factors, then convert back to a table.

Exercise 2.7 The data set `VisualAcuity` in `vcd` gives $4 \times 4 \times 2$ table as a frequency data frame.

```
data("VisualAcuity", package="vcd")
str(VisualAcuity)

## 'data.frame': 32 obs. of 4 variables:
## $ Freq : num 1520 234 117 36 266 ...
## $ right : Factor w/ 4 levels "1","2","3","4": 1 2 3 4 1 2 3 4 1 2 ...
## $ left : Factor w/ 4 levels "1","2","3","4": 1 1 1 1 2 2 2 2 3 3 ...
## $ gender: Factor w/ 2 levels "male","female": 2 2 2 2 2 2 2 2 2 2 ...
```

- From this, use `xtabs()` to create two 4×4 frequency tables, one for each gender.
- Use `structable()` to create a nicely organized tabular display.
- Use `xtable()` to create a \LaTeX or HTML table.

References

- Agresti, A. (2002). *Categorical Data Analysis*. Wiley Series in Probability and Statistics. New York: Wiley-Interscience [John Wiley & Sons], 2nd edn.
- Fox, J. and Weisberg, S. (2011). *An R Companion to Applied Regression*. Thousand Oaks CA: Sage, 2nd edn.
- Hartigan, J. A. and Kleiner, B. (1984). A mosaic of television ratings. *The American Statistician*, 38, 32–35.
- Koch, G. and Edwards, S. (1988). Clinical efficiency trials with categorical data. In K. E. Peace, ed., *Biopharmaceutical Statistics for Drug Development*, (pp. 403–451). New York: Marcel Dekker.
- Leifeld, P. (2013). texreg: Conversion of statistical model output in r to latex and html tables. *Journal of Statistical Software*, 55(8), 1–24.